Continuous Optimization

Examples and Applications

Formulate some practical problems in an optimization problem, **classify** it (convex or nonconvex or possible ways to make it convex) and **solve** it (analytically or numerically).

Minimal distance to discrete points (Least Square) Sum of squared distance:

$$\min_{x} \quad \sum_{i=1}^{n} \|x - x_i\|^2$$

Minimal distance to a subspace (Projection)

Find the minimal distance from a point x_0 to the intersection of the space spanned by the vectors v_1, v_2, \dots, v_m .

Minimal covering disk

Given points x_1, x_2, \dots, x_N , find a disk with minimal radius (centered at x_0 with radius R) such that $||x_0 - x_i|| \le R$.

Heron's problem

Find C on the line ℓ , such that |AC| + |BC| is minimal.

