

Curriculum Vitae of J. Toby Stafford

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Born: Oxford, England, June 2, 1951. *Nationality:* British

Positions Held:

1976-8 NATO Postdoctoral Research Fellow, Brandeis University;
1978-82 Davey Research Fellow, Gonville and Caius College, Cambridge, England;
1982-85 Lecturer, University of Leeds, England:
1985-88 Reader, University of Leeds, England:
1988-9 Personal Chair, University of Leeds, England:
1989–2007 Professor, University of Michigan, Ann Arbor.
2007–2018 Professor, University of Manchester.
2018–present Emeritus Professor, University of Manchester.

Visiting Positions:

May 1981 Université de Paris VI;
Sept. 1983 Wiezmann Institute;
July-Aug. 1982 Wiezmann Institute;
Sept.1980-June 1981 University of California, San Diego;
April-Dec. 1985 University of Washington;
Sept. 1986-June 1987 University of California, San Diego;
April-June 1988 University of Chicago;
Jan.-April 1996 MIT;
June 1996 Université de Poitiers;
June 1998 Université de Brest;
Jan.-May 2000 Mathematics Science Research Institute, Berkeley;
Nov.-Dec. 2003 Mittag-Leffler Institute;
Nov.-Dec. 2006 Newton Institute, Cambridge;
Jan.-Feb. 2011 Hausdorff Institute, Bonn;
Jan.-May 2013 Mathematics Science Research Institute, Berkeley;

Education and Degrees:

BA University of Cambridge, England, 1972;
 MA University of Cambridge, England, 1976;
 PhD University of Leeds, England, 1976 (advisor J. C. Robson).

Honours:

1980 Whitehead Prize, London Mathematical Society;
 1996 Excellence in Research Award, University of Michigan;
 2002 Invited Speaker, ICM (Beijing, August 2002);
 2007-2013 Royal Society-Wolfson Research Merit Award;
 2012-2013 Clay Senior Scholar and Simons Visiting Professor, MSRI, Berkeley;
 2013 Fellow of the American Mathematical Society.

Research Students:

Martin P Gilchrist (1982-1985) PhD 1985	S. Collier Coutinho (1982-1986) PhD 1986
Tim Jarrold (1986-1990) PhD 1990	David Kausch (1990-1993) PhD 1993
Darin Stephenson (1990-1994) PhD 1994	Kok-Ming Teo (1991-1994) PhD 1994
Paul Check (1994-1997) PhD 1997	Dennis Keeler (1997-2000) PhD 2000
Kimberley Retert (1997-2001) PhD 2001	Dan R. Rogalski (1998-2002) PhD 2002
Susan Sierra (2005-2008) PhD 2008	Chelsea Walton (2006-2011) PhD 2011
Sian Fryer (2010-2014) PhD 2014	Andrew Davies (2010-2014) PhD 2014
Dominic Bush-Hipwood (2014-2018) PhD 2018	

As first positions, Keeler, Rogalski and Walton all obtained NSF Postdocs and Moore Instructorships at MIT, while Sierra obtained an NSF Postdoc and Instructorship at Princeton.

Postdoctoral Advisees:

Martin Holland (1987-89),	James Zhang (1990-93),	Tony Giaquinto (1991-95),
Joanna Stanizskis (1994-97)	Ioannis Emmanouil (1995-98),	Daniel Chan (2000-02),
Jason Bell (2002-05),	Tatyana Chmutova (2006-07),	Gwyn Bellamy (2011-13).

NSF Grants Award Amount

1990-1993	\$166,200.00
1993-1998	\$416,400.00
1998-2003	\$329,185.00
2003-2006	\$230,049.00
2006-2011	\$460,000.00

Citations: **h-index** 21 (21 papers with at least 21 citations on the Web of Science.)
 Over 1,300 Web of Science citations;
 Over 950 citations on MathSciNet.

Editorial Boards:

- 1987–1988 London Mathematical Society;
- 1988–2018 Journal of Algebra;
- 1993–1996 Contemporary Mathematics;
- 2001–2008 AMS Surveys and Monographs (Chair 2005–08);
- 2007–2009 AMS University Lecture Notes Series;
- 2007–present Algebra and Number Theory;
- 2009–present LMS Lecture Note Series;

Conferences and Conference Organisation:

- 1999–2000 Organising Committee, MSRI year in Noncommutative Algebra;
- 2002 First Auslander Distinguished Lecturer, Northeastern University;
- 2002 Organising Committee, Oberwolfach conference in Noncommutative Algebra;
- 2003–4 Scientific Committee, Warwick Symposium on Noncommutative Algebra;
- 2004 Scientific Committee for conference at the Mittag-Leffler Institute;
- 2006 Organising Committee, Oberwolfach conference in Noncommutative Algebra;
- 2006 Organising Committee for conference in Ring Theory at Leeds University;
- 2008 & 2011 Organised ARTIN Conferences at Manchester;
- 2010 Organising Committee, Oberwolfach conference in Noncommutative Algebra;
- 2011 UCSB Distinguished Lecturer in the Mathematical Sciences;
- 2011 Scientific Committee for conference at Seattle, Washington;
- 2011 Scientific Committee for conference at Fudan University Shanghai;
- 2013 Chair of MSRI programme in NC Algebraic Geometry and Representation Theory;
- 2014 Organising Committee, Oberwolfach conference in Noncommutative Algebra;
- 2014 Scientific Committee for conference at Fudan University Shanghai;
- 2014–5 Organising Committee, Warwick Symposium on Derived Categories and Applications;
- 2018 Organising Committee, Oberwolfach conference in Noncommutative Algebra;

External Activities:

- 1995–2001 NSA Mathematical Sciences Advisory Panel;
- 2001–3 AMS Von Neumann Symposium Committee;
- 2001–2 AMS Cole Prize Committee;
- 2004 NSF Algebra, Number Theory and Combinatorics Review Panel;
- 2005–9 Member of the AMS Council;
- 2008 External Committee for Mathematics, Universities of Paris 6 and 7;
- 2008–10 LMS Prizes Committee;
- 2011 External Committee for Mathematics, University of Antwerp;

Publications.

- 1) Completely faithful modules and ideals of simple Noetherian rings, *Bull. London Math. Soc.* **8** (1976), 168–173.
- 2) (with Rosenberg, A.) Global dimension of Ore extensions, *in Algebra, topology, and category theory (a collection of papers in honor of Samuel Eilenberg)*, pp. 181–188. Academic Press, New York, 1976.
- 3) Stable structure of noncommutative Noetherian rings, *J. Algebra* **47** (1977), 244–267.
- 4) Weyl algebras are stably free, *J. Algebra* **48** (1977), 297–304.
- 5) A simple Noetherian ring not Morita equivalent to a domain., *Proc. Amer. Math. Soc.* **68** (1978), 159–160.
- 6) Stable structure of noncommutative Noetherian rings. II, *J. Algebra* **52** (1978), 218–235.
- 7) (with Krause, G. and Lenagan, T.) Ideal invariance and Artinian quotient rings, *J. Algebra* **55** (1978), 145–154.
- 8) Morita equivalence of simple Noetherian rings, *Proc. Amer. Math. Soc.* **74** (1979), 212–214.
- 9) Module structure of Weyl algebras, *J. London Math. Soc.* (2) **18** (1978), 429–442.
- 10) K -theory of Noetherian group rings, *in Ring theory (Proc. Conf., Univ. Waterloo, Waterloo, 1978)*, pp. 302–322, Lecture Notes in Math., **Vol. 734**, Springer, Berlin, 1979.
- 11) (with Brown, K. A. and Lenagan, T. H.) Weak ideal invariance and localisation *J. London Math. Soc.* **21** (1980), 53–61.
- 12) (with Brown, K. A. and Lenagan, T. H.) K -theory and stable structure of some Noetherian group rings, *Proc. London Math. Soc.* **42** (1981), 193–230.
- 13) On the regular elements of Noetherian rings, *in Ring theory (Proc. Antwerp Conf., 1978)*, pp. 257–277, Lecture Notes in Pure and Appl. Math., **Vol. 51**, Dekker, New York, 1979.
- 14) Projective modules over polynomial extensions of division rings, *Inventiones Math.* **59** (1980), 105–117.
- 15) Bounded number of generations of right ideals in polynomial rings, *Comm. Algebra* **8** (1980), 1513–1518.
- 16) On the stable range of right Noetherian rings, *Bull. London Math. Soc.* **13** (1981), 39–41.
- 17) (with Cortzen, B. and Small, L. W.) Decomposing overrings, *Proc. Amer. Math. Soc.* **82** (1981), 28–30.
- 18) (with Small, L. W.) Localisation and completions of Noetherian PI algebras, *J. Algebra* **70** (1981), no. 1, 156–161.
- 19) Generating modules efficiently: algebraic K -theory for noncommutative Noetherian rings, *J. Algebra* **69** (1981), no. 2, 312–346; Corrig., *J. Algebra* **82** (1983), no. 1, 294–296.
- 20) Cancellation for nonprojective modules, *in Module theory (Proc. Special Session, Amer. Math. Soc., Univ. Washington, Seattle, Wash., 1977)*, pp. 3–15, Lecture Notes in Math., **Vol. 700**, Springer, Berlin, 1979.

- 21) (with Farkas, D. R., Schofield, A. H. and Snider, R. L.) The isomorphic question for division rings of group rings, *Proc. Amer. Math. Soc.* **85** (1982), 327–330.
- 22) Generating modules efficiently over noncommutative rings *in Paul Dubreil and Marie-Paule Malliavin Algebra Seminar*, (Paris, 1981), pp. 72–88, Lecture Notes in Math., **Vol. 924**, Springer, Berlin-New York, 1982.
- 23) (with Wallach, N. R.) The restriction of admissible modules to parabolic subalgebras, *Trans. Amer. Math. Soc.* **272** (1982), 333–350.
- 24) Homological properties of the enveloping algebra $U(\mathrm{Sl}_2)$, *Math. Proc. Cambridge Philos. Soc.* **91** (1982), 29–37.
- 25) (with Small, L. W.) Regularity of zero divisors, *Proc. London Math. Soc.* **44** (1982), 405–419.
- 26) Noetherian full quotient rings, *Proc. London Math. Soc.* **44** (1982), 385–404.
- 27) Rings with a bounded number of generators for right ideals, *Quart. J. Math. Oxford Ser.* **34** (1983), 107–114.
- 28) (with Resco, R. and Small, L. W.) Krull and global dimensions of semiprime Noetherian PI-rings, *Trans. Amer. Math. Soc.* **274** (1982), 285–295.
- 29) Dimensions of division rings, *Israel J. Math.* **45** (1983), 33–40.
- 30) (with Warfield, R. B., Jr.) Hereditary orders with infinitely many idempotent ideals, *J. Pure Appl. Algebra* **31** (1984), 217–225.
- 31) (with Joseph, A.) Modules of \mathfrak{k} -finite vectors over semisimple Lie algebras, *Proc. London Math. Soc.* **49** (1984), 361–384.
- 32) On the ideals of a Noetherian ring, *Trans. Amer. Math. Soc.* **289** (1985), 381–392.
- 33) (with Small, L. W. and Warfield, R. B., Jr.) Affine algebras of Gelfand-Kirillov dimension one are PI, *Math. Proc. Cambridge Philos. Soc.* **97** (1985), 407–414.
- 34) The Weyl algebra and finite-dimensional filtering, *Stochastics* **14** (1984), 29–31.
- 35) Nonholonomic modules over Weyl algebras and enveloping algebras, *Inventiones Math.* **79** (1985), 619–638.
- 36) Stably free, projective right ideals, *Compositio Math.* **54** (1985), 63–78.
- 37) (with Warfield, R. B., Jr.) Constructions of hereditary Noetherian rings and simple rings, *Proc. London Math. Soc.* **51** (1985), 1–20.
- 38) (with Small, L. W.) Homological properties of generic matrix rings, *Israel J. Math.* **51** (1985), 27–32.
- 39) Modules over prime Krull rings, *J. Algebra* **95** (1985), 332–342.
- 40) (with Resco, R. and Warfield, R. B., Jr.) Fully bounded G -rings, *Pacific J. Math.* **124** (1986), 403–415.
- 41) Endomorphisms of right ideals of the Weyl algebra, *Trans. Amer. Math. Soc.* **299** (1987), 623–639.
- 42) The Goldie rank of a module, *in Noetherian rings and their applications* (Oberwolfach, 1983), 1–20, Math. Surveys Monographs, **Vol. 24**, Amer. Math. Soc., Providence, RI, 1987.

- 43) Global dimension of semiprime Noetherian rings, *in Séminaire d'algèbre Paul Dubreil et Marie-Paule Malliavin* (Paris, 1986), 247–260, Lecture Notes in Math., **Vol. 1296**, Springer, Berlin-New York, 1987.
- 44) (with Smith, S. P.) Differential operators on an affine curve, *Proc. London Math. Soc.* **56** (1988), 229–259.
- 45) (with Chamarié, M.) When rings of differential operators are maximal orders, *Math. Proc. Cambridge Philos. Soc.* **102** (1987), 399–410.
- 46) (with Dean, C.) A nonembeddable Noetherian ring, *J. Algebra* **115** (1988), 175–181.
- 47) (with Levasseur, T. and Smith, S. P.) The minimal nilpotent orbit, the Joseph ideal, and differential operators, *J. Algebra* **116** (1988), 480–501.
- 48) (with Hodges, T. J.) Noetherian rings with big indecomposable projective modules, *Bull. London Math. Soc.* **21** (1989), 249–254.
- 49) (with McConnell, J. C.) Gelfand-Kirillov dimension and associated graded modules, *J. Algebra* **125** (1989), 197–214.
- 50) (with Levasseur, T.) Rings of differential operators on classical rings of invariants, *Mem. Amer. Math. Soc.* **81** (1989), no. 412, vi+117 pp.
- 51) Yet more indecomposable projectives over PI rings, *in Ring theory 1989* (Ramat Gan and Jerusalem, 1988/1989), 48–52, Israel Math. Conf. Proc., **Vol.1**, Weizmann, Jerusalem, 1989.
- 52) A nil implies nilpotent theorem for left ideals, *J. Algebra* **133** (1990), 545–549.
- 53) Absolute stable rank and quadratic forms over noncommutative rings, *K-Theory* **4** (1990), 121–130.
- 54) (with Holland, M. P.) Differential operators on rational projective curves, *J. Algebra* **147** (1992), 176–244.
- 55) (with Goodearl, K. R.) Warfield in ring theory, *in Abelian groups and noncommutative rings*, 11–15, Contemp. Math., **Vol. 130**, Amer. Math. Soc., Providence, RI, 1992.
- 56) (with Smith, S. P.) Regularity of the four-dimensional Sklyanin algebra, *Compositio Math.* **83** (1992), 259–289.
- 57) (with Levasseur, T.) The quantum coordinate ring of the special linear group, *J. Pure Appl. Algebra* **86** (1993), 181–186.
- 58) Regularity of algebras related to the Sklyanin algebra, *Trans. Amer. Math. Soc.* **341** (1994), 895–916.
- 59) (with Levy, L. S. and Robson, J. C.) Hidden matrices, *Proc. London Math. Soc. (3)* **69** (1994), 277–308.
- 60) (with Levasseur, T.) Invariant differential operators and an homomorphism of Harish-Chandra, *J. Amer. Math. Soc.* **8** (1995), 365–372.
- 61) (with Zhang, J. J.) Examples in non-commutative projective geometry, *Math. Proc. Cambridge Philos. Soc.* **116** (1994), 415–433.
- 62) (with Zhang, J. J.) Homological properties of (graded) Noetherian PI rings, *J. Algebra* **168**

- (1994), 988–1026.
- 63) Auslander-regular algebras and maximal orders, *J. London Math. Soc. (2)* **50** (1994), 276–292.
- 64) (with Artin, M.) Noncommutative graded domains with quadratic growth, *Inventiones Math.* **122** (1995), 231–276.
- 65) (with Levasseur, T.) The kernel of an homomorphism of Harish-Chandra, *Ann. Sci. Ecole Norm. Sup. (4)* **29** (1996), 385–397.
- 66) (with Levasseur, T.) Differential operators commuting with invariant functions, *Comment. Math. Helv.* **72** (1997), 426–433.
- 67) (with Levasseur, T.) Semi-simplicity of invariant holonomic systems on a reductive Lie algebra, *Amer. J. Math.* **119** (1997), 1095–1117.
- 68) (with Levasseur, T.) Invariant differential operators on the tangent space of some symmetric spaces, *Annales de l’Institut Fourier (Grenoble)* **49** (1999), 1711–1741.
- 69) (with Levasseur, T.) Differential operators on some nilpotent orbits, *Represent. Theory* **3** (1999), 457–473.
- 70) (with Artin, M.) Semiprime graded algebras of dimension two, *J. Algebra* **227** (2000), 68–123.
- 71) (with Goodearl, K. R.) The graded version of Goldie’s theorem, *Contemp. Math.* **259** (2000), 237–240.
- 72) (with Van den Bergh, M.) Noncommutative projective curves and surfaces, *Bull. Amer. Math. Soc.* **38** (2001), 171–216.
- 73) Noncommutative projective geometry, *Proceedings of the International Congress of Mathematicians*, Vol. II (Beijing, 2002), 93–103, Higher Ed. Press, Beijing, 2002.
- 74) (with Zhang, J. J.) Algebras without noetherian filtrations, *Proc. Amer. Math. Soc.* **131** (2003), 1329–1338.
- 75) (with Goodearl, K. R.) Simplicity of noncommutative Dedekind domains, *Proc. Amer. Math. Soc.* **133** (2005), 681–686.
- 76) (with Keeler D. and Rogalski D.) Naïve noncommutative blowing up, *Duke Math. J.* **126** (2005), 491–546.
- 77) (with Gordon I.) Cherednik algebras and Hilbert schemes of points, *Advances in Math.* **198** (2005), 222–274.
- 78) (with Gordon I.) Cherednik algebras and Hilbert schemes of points II: representations and sheaves, *Duke Math. J.* **132** (2006), 73–135.
- 79) (with Levasseur T.) Differential operators and cohomology groups on the basic affine space, pp. 377–405, in *Studies in Lie Theory*, Eds. J. Bernstein et al, Progress in Math., Birkhäuser, Boston, 2006.
- 80) (with Nevins T.) Sklyanin algebras and Hilbert schemes of points, *Advances in Math.* **210** No.1 (2007) 405–478.
- 81) (with Rogalski, D.) Naïve noncommutative blowups at zero dimensional schemes, *J. Algebra*, **318** (2007), 794–833.

- 82) (with Van den Bergh M.) Noncommutative resolutions and rational singularities, *Michigan Math. J.*, **57** (2008), 659-674.
- 83) (with Rogalski D.) A class of noncommutative projective surfaces, *Proc. London Math. Soc.*, **99** (2009), 100-144.
- 84) (with Ginzburg V. and Gordon I.) Differential operators and Cherednik algebras, *Selecta Math.*, **14** (2009), 629–666.
- 85) Generating regular elements, *C. R. Acad. Sci. Paris* **351** (2013), 429-432.
- 86) (with Rogalski D. and Sierra S. J.) Algebras in which every subalgebra is noetherian, *Proc. Amer. Math. Soc.* **142** (2014), 2983-2990.
- 87) (with Gordon I.) The Auslander property for Z -algebras, *J. Algebra* **399** (2014), 102-130.
- 88) (with Rogalski D. and Sierra S. J.) Classifying orders in the Sklyanin algebra, *Algebra and Number Theory* **9** (2015), 2056-2119.
- 89) (with Rogalski D. and Sierra S. J.) Noncommutative blowups of elliptic algebras, *Algebras and Rep. Theory* **18** (2015), 491-529.
- 90) (with Levasseur T.) Higher symmetries of powers of the Laplacian and rings of differential operators, *Compositio Math.*, **153** (2017), 678-716.
- 91) (with Rogalski D. and Sierra S. J.) Ring-theoretic blowing down; I, *J. Noncommutative Geometry*, **11** (2017), 1465-1520.
- 92) (with Rogalski D. and Sierra S. J.) Noncommutative minimal surfaces, preprint (2018), see arxiv:1807.09889.

Books and Conference Proceedings

- 1) (edited with Fuchs L., Goodearl K. R. and Vinsonhaler C.) *Abelian groups and noncommutative rings. A collection of papers in memory of Robert B. Warfield, Jr.* Contemporary Mathematics, 130. American Mathematical Society, Providence, RI, 1992. x+394 pp.
- 2) (edited with Ara P., Brown K., ; Lenagan T., Letzter E. and Zhang J.), *New trends in noncommutative algebra*, Contemp. Math., **562**, Amer. Math. Soc., Providence, RI, 2012.
- 3) (edited with Eisenbud D., Iyengar S. B., Singh A. K. and Van den Bergh v) *Commutative Algebra and Noncommutative Geometry; Vol. 1. Expository Articles*, (MSRI Publications), CUP, Cambridge, England, 2015.
- 4) (edited with Eisenbud D., Iyengar S. B., Singh A. K. and Van den Bergh) *Commutative Algebra and Noncommutative Geometry; Vol. 2. Research Articles*, (MSRI Publications), CUP, Cambridge, England, 2015.
- 5) (with Bellamy G., Rogalski D., Schedler T. and Wemyss M.) *Noncommutative Algebraic Geometry*, (MSRI Publications), CUP, Cambridge, England, 2016.