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■ 72 students better than the average.
■ 2 tests received without name.
■ Student 9023503 not registered?

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$\square(A+B)^{2} \neq A^{2}+2 A B+B^{2}$ in general.

