

Solutions for Session 6

08/11/2022

```
. do solution.do
. global basedir http://personalpages.manchester.ac.uk/staff/mark.lunt
. global datadir $basedir/stats/6_LinearModels2/data
. sysuse auto, clear
(1978 Automobile Data)
```

```
. regress weight foreign
```

Source	SS	df	MS			
Model	15496779.3	1	15496779.3	Number of obs =	74	
Residual	28597399.1	72	397186.099	F(1, 72) =	39.02	
Total	44094178.4	73	604029.841	Prob > F =	0.0000	
				R-squared =	0.3514	
				Adj R-squared =	0.3424	
				Root MSE =	630.23	

weight	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
foreign	-1001.206	160.2876	-6.25	0.000	-1320.734	-681.6788
_cons	3317.115	87.39676	37.95	0.000	3142.893	3491.338

*1.1 foreign vehicles are, on average, 1000 lbs lighter than US vehicles
The difference is significant, p = 0.000*

```
. regress weight i.foreign
```

Source	SS	df	MS			
Model	15496779.3	1	15496779.3	Number of obs =	74	
Residual	28597399.1	72	397186.099	F(1, 72) =	39.02	
Total	44094178.4	73	604029.841	Prob > F =	0.0000	
				R-squared =	0.3514	
				Adj R-squared =	0.3424	
				Root MSE =	630.23	

weight	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
foreign	-1001.206	160.2876	-6.25	0.000	-1320.734	-681.6788
Foreign	-1001.206	160.2876	-6.25	0.000	-1320.734	-681.6788
_cons	3317.115	87.39676	37.95	0.000	3142.893	3491.338

1.2 This makes no difference at all

```
. ttest weight, by(foreign)
Two-sample t test with equal variances
```

Group	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
Domestic	52	3317.115	96.4296	695.3637	3123.525	3510.706
Foreign	22	2315.909	92.31665	433.0035	2123.926	2507.892
combined	74	3019.459	90.34692	777.1936	2839.398	3199.521
diff		1001.206	160.2876		681.6788	1320.734

```
diff = mean(Domestic) - mean(Foreign)          t = 6.2463
Ho: diff = 0                                   degrees of freedom = 72
Ha: diff < 0                                  Ha: diff != 0                Ha: diff > 0
Pr(T < t) = 1.0000                            Pr(|T| > |t|) = 0.0000        Pr(T > t) = 0.0000
```

1.3 the mean difference and standard error are exactly the same (except for the minus sign)

```
. graph box weight, over(foreign)

. graph export graph1.eps replace
(file graph1.eps written in EPS format)
```

1.4 There is a wider spread of weights for Domestic cars compared to Foreign cars, i.e. greater variance

```
. by foreign: summ weight
```

```
-> foreign = Domestic
```

Variable	Obs	Mean	Std. Dev.	Min	Max
weight	52	3317.115	695.3637	1800	4840

```
-> foreign = Foreign
```

Variable	Obs	Mean	Std. Dev.	Min	Max
weight	22	2315.909	433.0035	1760	3420

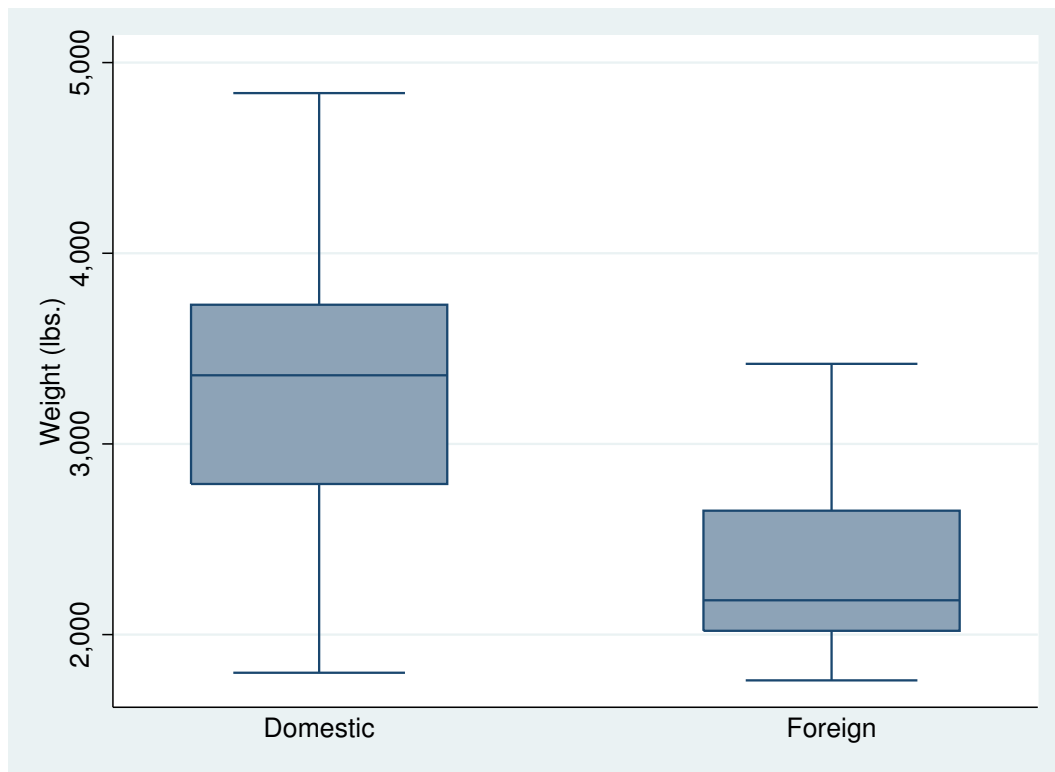


Figure 1: . graph box weight, over(foreign)

1.5 the SD is much higher for Domestic (~700) compared to Foreign (~430)

```
. hetttest
Breusch-Pagan / Cook-Weisberg test for heteroskedasticity
Ho: Constant variance
Variables: fitted values of weight
chi2(1)      =    4.51
Prob > chi2  =   0.0337
```

1.6 The difference in variance is significant. Therefore, a linear model is inappropriate

```
. use $datadir/soap, clear
. graph box appearance, over(operator)
```

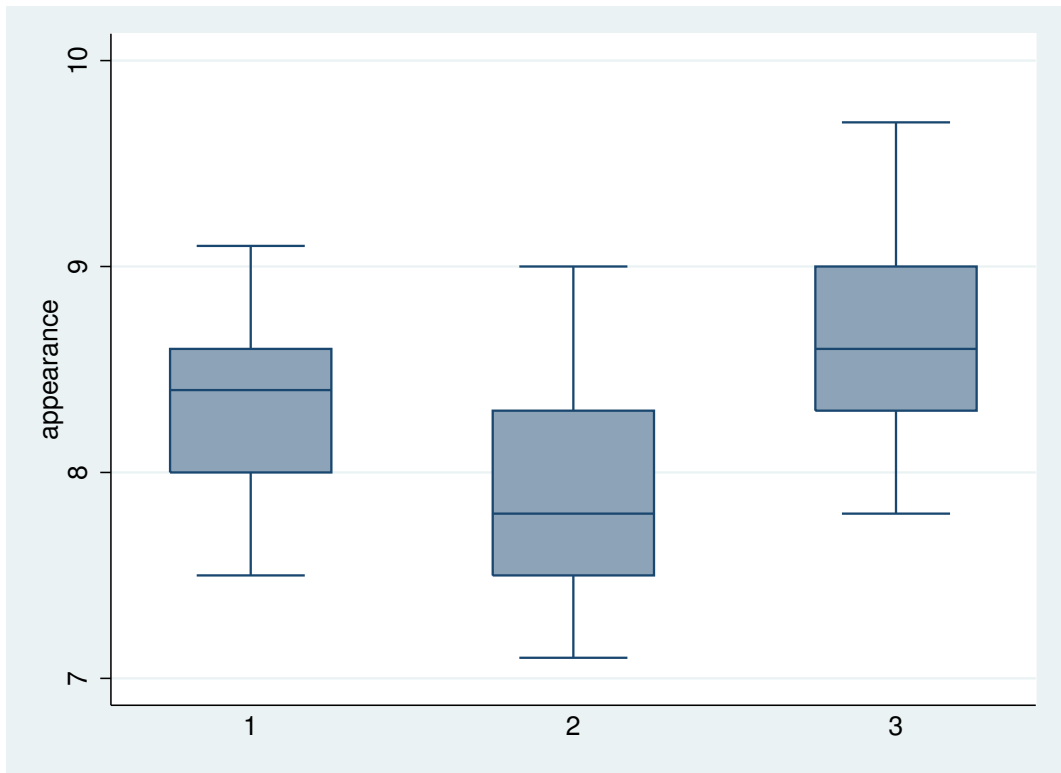


Figure 2: . graph box appearance, over(operator)

```
. graph export graph2.eps replace  
(file graph2.eps written in EPS format)
```

1.7 Operator 3 has the highest scores: 25% of scores are above 9

```
. sort operator
```

. by operator: summ appearance

-> operator = 1

Variable	Obs	Mean	Std. Dev.	Min	Max
appearance	30	8.306667	.4630732	7.5	9.1

-> operator = 2

Variable	Obs	Mean	Std. Dev.	Min	Max
appearance	30	7.896667	.4766863	7.1	9

-> operator = 3

Variable	Obs	Mean	Std. Dev.	Min	Max
appearance	30	8.626667	.4653018	7.8	9.7

. regress appearance i.operator

Source	SS	df	MS			
Model	8.03400033	2	4.01700016	Number of obs =	90	
Residual	19.0869988	87	.219390791	F(2, 87) =	18.31	
Total	27.1209991	89	.304730327	Prob > F	= 0.0000	
				R-squared	= 0.2962	
				Adj R-squared	= 0.2800	
				Root MSE	= .46839	

appearance	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
operator						
2	-.41	.1209382	-3.39	0.001	-.6503778	-.1696222
3	.3200001	.1209382	2.65	0.010	.0796223	.5603779
_cons	8.306667	.0855162	97.14	0.000	8.136694	8.476639

1.9 Yes: Prob > F = 0.0000 is testing the null hypothesis that all operators are the same.

1.10 $p = 0.0000$

1.11 Operator 1 is the baseline: there is no line for operator 1

. lincom _cons + 2.operator

(1) 2.operator + _cons = 0

appearance	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
(1)	7.896667	.0855162	92.34	0.000	7.726694	8.066639

1.12 This is the same as we have already seen

```
. lincom 2.operator - 3.operator
( 1) 2.operator - 3.operator = 0
```

appearance	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
(1)	-.73	.1209382	-6.04	0.000	-.9703778 - .4896222

1.13 Yes: $t = -6.04$, $p = 0.000$

```
. use $datadir/cadmium, clear
. scatter capacity age
```

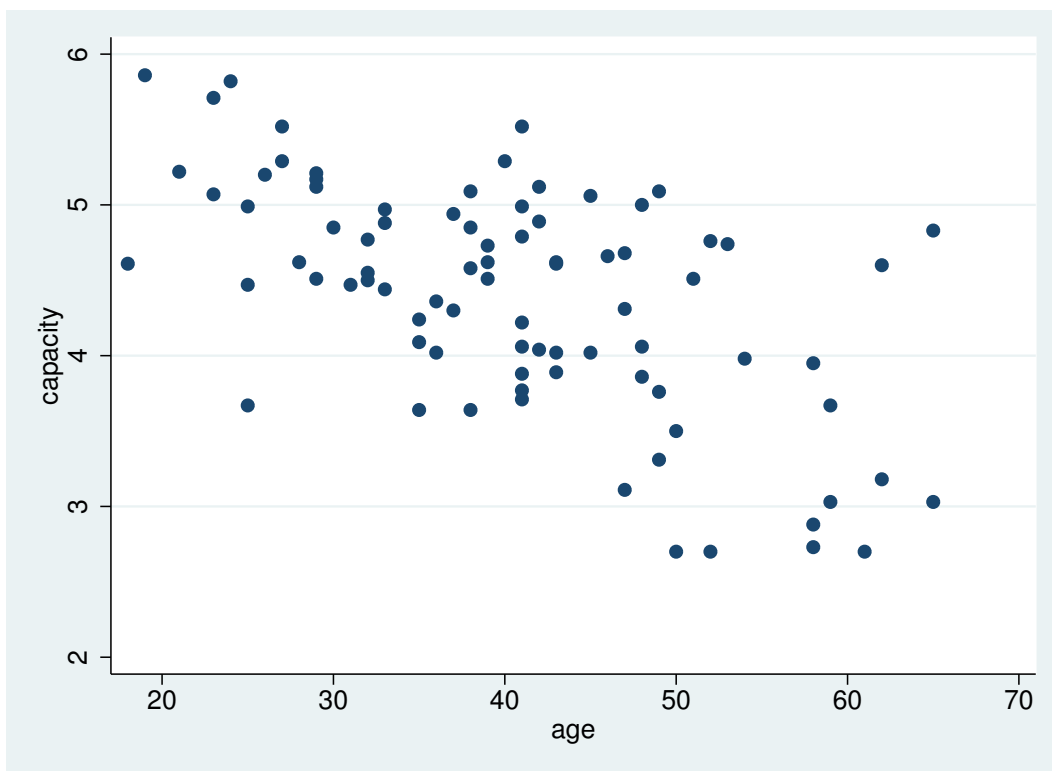


Figure 3: . scatter capacity age

```
. graph export graph3.eps replace
(file graph3.eps written in EPS format)
```

```
. regress capacity age
```

Source	SS	df	MS			
Model	17.4445864	1	17.4445864	Number of obs =	84	
Residual	30.1963679	82	.368248388	F(1, 82) =	47.37	
Total	47.6409543	83	.573987401	Prob > F =	0.0000	
				R-squared =	0.3662	
				Adj R-squared =	0.3584	
				Root MSE =	.60683	

capacity	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
age	-.0404781	.0058811	-6.88	0.000	-.0521776	-.0287787
_cons	6.033316	.247487	24.38	0.000	5.540986	6.525647

2.2 The regression coefficient for age is negative, showing that capacity decreases as age increases.

```
. gen cap1 = capacity if exposure == 1
(40 missing values generated)

. gen cap2 = capacity if exposure == 2
(56 missing values generated)

. gen cap3 = capacity if exposure == 3
(72 missing values generated)

. scatter cap1 cap2 cap3 age

. graph export graph4.eps replace
(file graph4.eps written in EPS format)
```

```
. regress capacity i.exposure
```

Source	SS	df	MS			
Model	2.74733751	2	1.37366875	Number of obs =	84	
Residual	44.8936168	81	.554242182	F(2, 81) =	2.48	
Total	47.6409543	83	.573987401	Prob > F =	0.0902	
				R-squared =	0.0577	
				Adj R-squared =	0.0344	
				Root MSE =	.74447	

capacity	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
exposure						
< 10 years	.0097403	.1799744	0.05	0.957	-.3483523	.3678329
> 10 years	-.5128788	.2424526	-2.12	0.037	-.9952834	-.0304741
_cons	4.462045	.1122337	39.76	0.000	4.238735	4.685355

2.3 Its borderline, $p = 0.09$

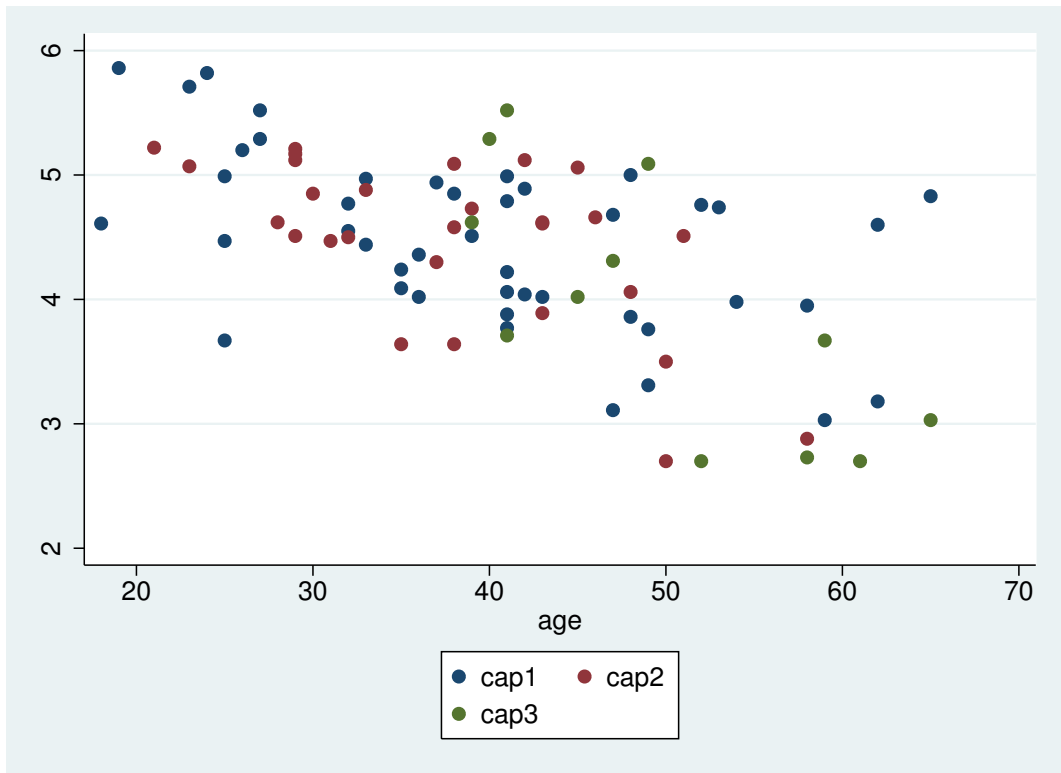


Figure 4: . scatter cap1 cap2 cap3 age

```
. regress capacity age i.exposure
```

Source	SS	df	MS			
Model	17.6062849	3	5.86876164	Number of obs =	84	
Residual	30.0346693	80	.375433367	F(3, 80) =	15.63	
Total	47.6409543	83	.573987401	Prob > F =	0.0000	
				R-squared =	0.3696	
				Adj R-squared =	0.3459	
				Root MSE =	.61273	

capacity	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
age	-.0397752	.0063224	-6.29	0.000	-.0523572	-.0271931
exposure						
< 10 years	-.0701975	.1486686	-0.47	0.638	-.3660575	.2256626
> 10 years	-.1169349	.2092361	-0.56	0.578	-.5333281	.2994582
_cons	6.044917	.2680248	22.55	0.000	5.51153	6.578303


```

. testparm i.exposure
( 1) 2.exposure = 0
( 2) 3.exposure = 0
      F( 2, 80) = 0.22
      Prob > F = 0.8067

```

2.4 There are now no significant differences between groups

```

. predict ppred, xb

. gen ppred1 = ppred if exposure == 1
(40 missing values generated)

. gen ppred2 = ppred if exposure == 2
(56 missing values generated)

. gen ppred3 = ppred if exposure == 3
(72 missing values generated)

. scatter cap1 cap2 cap3 age || line ppred1 age || line ppred2 age || /* */
line ppred3 age

```

```

. graph export graph5.eps replace
(file graph5.eps written in EPS format)

```

```

. regress capacity i.exposure##c.age

```

Source	SS	df	MS			
Model	20.1057424	5	4.02114849	Number of obs =	84	
Residual	27.5352118	78	.353015536	F(5, 78) =	11.39	
Total	47.6409543	83	.573987401	Prob > F =	0.0000	
				R-squared =	0.4220	
				Adj R-squared =	0.3850	
				Root MSE =	.59415	

capacity	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
exposure						
< 10 years	.5497403	.5758844	0.95	0.343	-.5967574	1.696238
> 10 years	2.503148	1.041842	2.40	0.019	.4289997	4.577296
age	-.0306127	.0075475	-4.06	0.000	-.0456385	-.0155868
exposure#c.age						
< 10 years	-.0159193	.0145469	-1.09	0.277	-.0448799	.0130413
> 10 years	-.0544983	.0210698	-2.59	0.012	-.0964451	-.0125516
_cons	5.680291	.313426	18.12	0.000	5.056307	6.304274

```

. testparm i.exposure#c.age
( 1) 2.exposure#c.age = 0
( 2) 3.exposure#c.age = 0
      F( 2, 78) = 3.54
      Prob > F = 0.0338

```

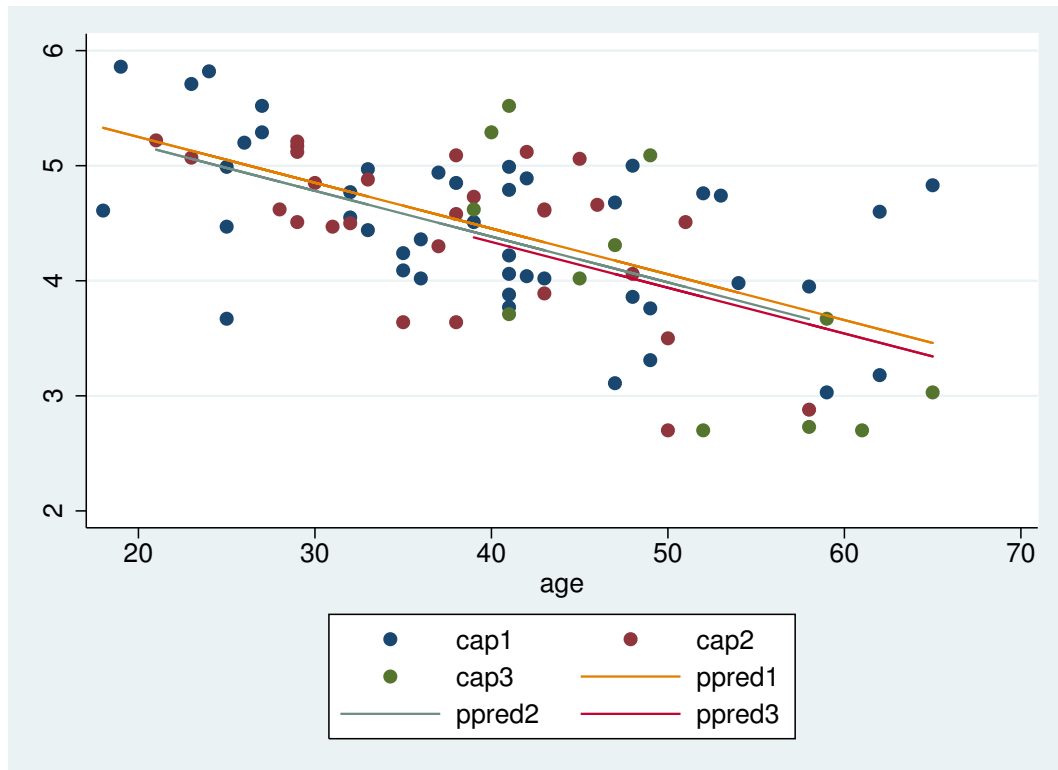


Figure 5: `. scatter cap1 cap2 cap3 age — line ppred1 age — line ppred2 age — /*`

2.5 Yes, the slopes in the different exposure groups are different

```
. predict ipred, xb
. gen ipred1 = ipred if exposure == 1
(40 missing values generated)
. gen ipred2 = ipred if exposure == 2
(56 missing values generated)
. gen ipred3 = ipred if exposure == 3
(72 missing values generated)
. scatter cap1 cap2 cap3 age || line ipred1 age || line ipred2 age || /* */
line ipred3 age
```

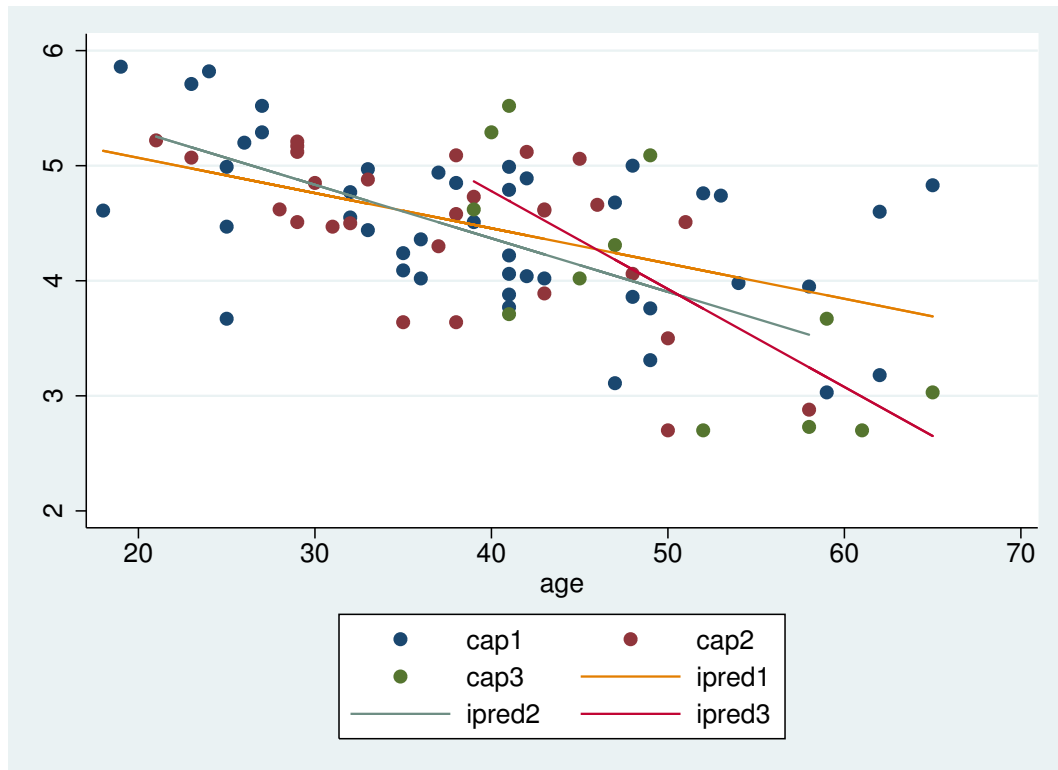


Figure 6: . scatter cap1 cap2 cap3 age — line ipred1 age — line ipred2 age — /*

```
. graph export graph6.eps replace
(file graph6.eps written in EPS format)
```

*2.6 The least steep is in the baseline (least exposed group)
The steepest is in the most exposed group*

```
. lincom age + 3.exposure#c.age
( 1) age + 3.exposure#c.age = 0
```

capacity	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
(1)	-.085111	.0196716	-4.33	0.000	-.1242742 -.0459478

```
. use $datadir/hald, clear
```

```
. sw regress y x1 x2 x3 x4, pe(0.05)
      begin with empty model
p = 0.0006 < 0.0500 adding x4
p = 0.0000 < 0.0500 adding x1
```

Source	SS	df	MS
Model	2641.00094	2	1320.50047
Residual	74.7621108	10	7.47621108
Total	2715.76305	12	226.313587

```
Number of obs = 13
F( 2, 10) = 176.63
Prob > F = 0.0000
R-squared = 0.9725
Adj R-squared = 0.9670
Root MSE = 2.7343
```

y	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
x4	-.6139536	.0486446	-12.62	0.000	-.7223404 - .5055668
x1	1.439958	.1384166	10.40	0.000	1.131547 1.74837
_cons	103.0974	2.123984	48.54	0.000	98.36485 107.8299

3.1 x1 & x4 are retained

```
. sw regress y x1 x2 x3 x4, pr(0.05)
      begin with full model
p = 0.8959 >= 0.0500 removing x3
p = 0.2054 >= 0.0500 removing x4
```

Source	SS	df	MS
Model	2657.85857	2	1328.92929
Residual	57.9044793	10	5.79044793
Total	2715.76305	12	226.313587

```
Number of obs = 13
F( 2, 10) = 229.50
Prob > F = 0.0000
R-squared = 0.9787
Adj R-squared = 0.9744
Root MSE = 2.4063
```

y	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]
x1	1.468306	.1213009	12.10	0.000	1.19803 1.738581
x2	.6622505	.0458547	14.44	0.000	.5600798 .7644212
_cons	52.57735	2.286174	23.00	0.000	47.48344 57.67126

3.2 This time x1 & x2 are retained

```
. sw regress y x1 x2 x3 x4, pe(0.05) pr(0.0500005)
      begin with full model
p = 0.8959 >= 0.0500 removing x3
p = 0.2054 >= 0.0500 removing x4
```

Source	SS	df	MS			
Model	2657.85857	2	1328.92929	Number of obs =	13	
Residual	57.9044793	10	5.79044793	F(2, 10) =	229.50	
Total	2715.76305	12	226.313587	Prob > F =	0.0000	
				R-squared =	0.9787	
				Adj R-squared =	0.9744	
				Root MSE =	2.4063	

y	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
x1	1.468306	.1213009	12.10	0.000	1.19803	1.738581
x2	.6622505	.0458547	14.44	0.000	.5600798	.7644212
_cons	52.57735	2.286174	23.00	0.000	47.48344	57.67126

3.3 This is the same as the backwards model

```
. corr x*
(obs=13)
```

	x1	x2	x3	x4
x1	1.0000			
x2	0.2286	1.0000		
x3	-0.8241	-0.1392	1.0000	
x4	-0.2454	-0.9730	0.0295	1.0000

3.4 Correlation between x2 & x4 is -0.97

3.5 x2 & x4 are very strongly correlated: they contain the same information, so they are largely interchangeable

```
. regress y x1 x2 x3 x4
```

Source	SS	df	MS			
Model	2667.89941	4	666.974853	Number of obs =	13	
Residual	47.863637	8	5.98295463	F(4, 8) =	111.48	
Total	2715.76305	12	226.313587	Prob > F =	0.0000	
				R-squared =	0.9824	
				Adj R-squared =	0.9736	
				Root MSE =	2.446	

y	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
x1	1.551103	.7447698	2.08	0.071	-.1663395	3.268545
x2	.5101677	.723788	0.70	0.501	-1.15889	2.179226
x3	.1019096	.754709	0.14	0.896	-1.638453	1.842272
x4	-.1440609	.709052	-0.20	0.844	-1.779138	1.491016
_cons	62.40535	70.07096	0.89	0.399	-99.17856	223.9893

3.6 The F statistic says that the model is very highly significant: the null hypothesis that all coefficients are 0 could not have given rise to this data
3.7 98% of the variance is explained
3.8 None of the coefficients are significant, due to the strong correlations between them

```
. use $datadir/growth, clear  
. scatter weight week
```

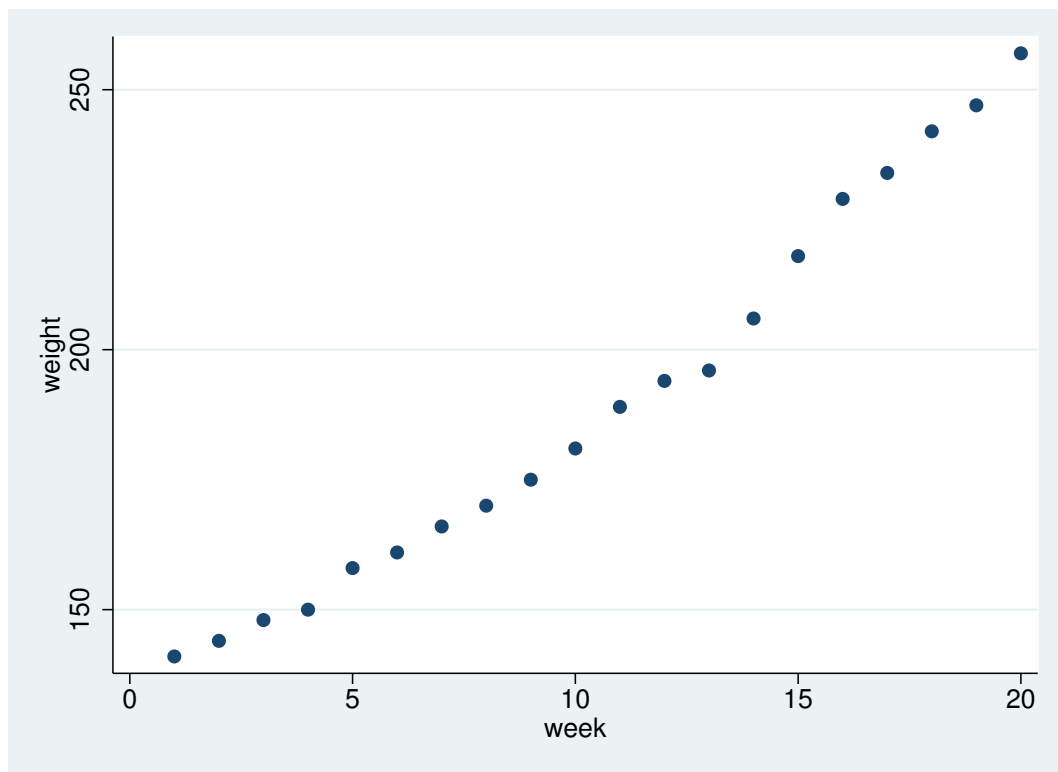


Figure 7: . scatter weight week

```
. graph export graph7.eps replace  
(file graph7.eps written in EPS format)
```

4.1 The line does not look quite straight: there appears to be some curvature

```
. regress weight week
```

Source	SS	df	MS				
Model	25438.7504	1	25438.7504	Number of obs = 20			
Residual	579.449624	18	32.1916458	F(1, 18) = 790.23			
Total	26018.2	19	1369.37895	Prob > F = 0.0000			
				R-squared = 0.9777			
				Adj R-squared = 0.9765			
				Root MSE = 5.6738			

weight	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
week	6.184962	.2200193	28.11	0.000	5.722719	6.647206
_cons	125.3579	2.635644	47.56	0.000	119.8206	130.8952

```
. cprplot week
```

4.2 There is definitely curvature around the line

```
. gen week2 = week * week
```

```
. regress weight week week2
```

Source	SS	df	MS				
Model	25927.7513	2	12963.8756	Number of obs = 20			
Residual	90.4487127	17	5.32051251	F(2, 17) = 2436.58			
Total	26018.2	19	1369.37895	Prob > F = 0.0000			
				R-squared = 0.9965			
				Adj R-squared = 0.9961			
				Root MSE = 2.3066			

weight	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
week	2.680178	.3763642	7.12	0.000	1.886119	3.474237
week2	.1668945	.0174086	9.59	0.000	.1301656	.2036235
_cons	138.2088	1.716086	80.54	0.000	134.5881	141.8294

4.3 week2 is very highly significant (p = 0.000)

```
. predict pred2, xb
```

```
. twoway scatter weight week || line pred2 week
```



```
. graph export graph8.eps replace
```

(file graph8.eps written in EPS format)

4.4 Curved predictor fits the data very well

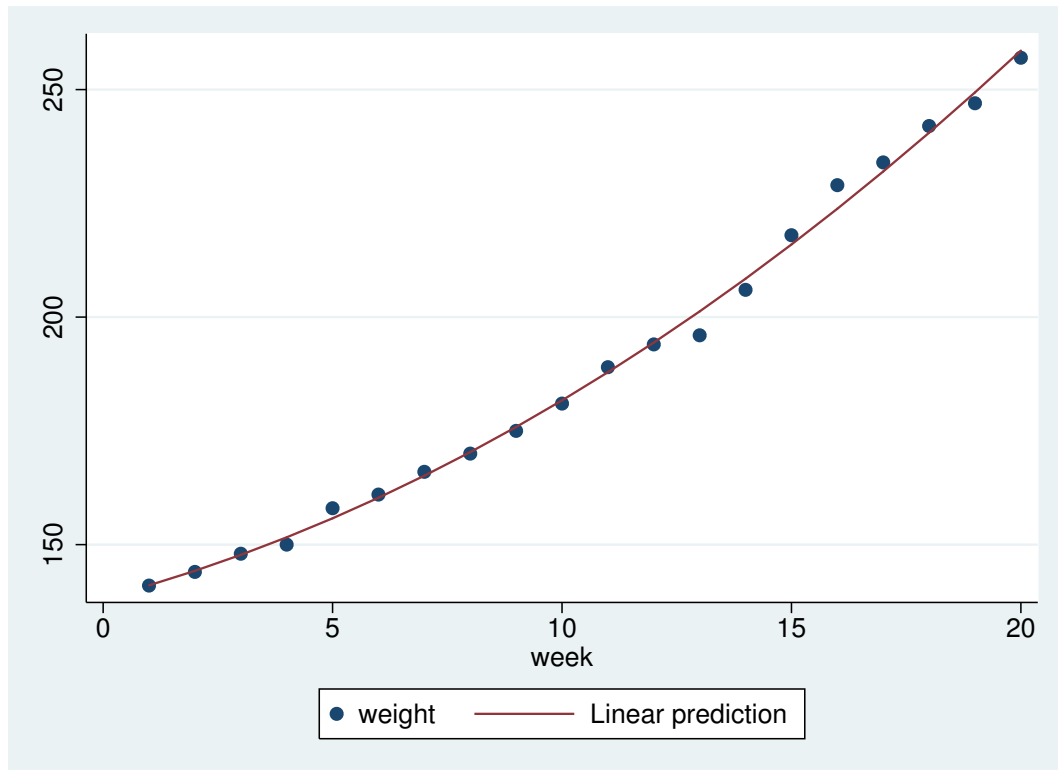


Figure 8: . twoway scatter weight week — line pred2 week

```
. gen week3 = week2*week
. regress weight week week2 week3
```

Source	SS	df	MS			
Model	25928.9007	3	8642.96691	Number of obs =	20	
Residual	89.2992705	16	5.58120441	F(3, 16) =	1548.58	
Total	26018.2	19	1369.37895	Prob > F =	0.0000	
				R-squared =	0.9966	
				Adj R-squared =	0.9959	
				Root MSE =	2.3625	

weight	Coef.	Std. Err.	t	P> t	[95% Conf. Interval]	
week	2.242641	1.038333	2.16	0.046	.0414737	4.443808
week2	.2177334	.1134353	1.92	0.073	-.0227388	.4582055
week3	-.0016139	.0035564	-0.45	0.656	-.0091531	.0059252
_cons	139.0663	2.580587	53.89	0.000	133.5957	144.5369

4.5 week3 is not significant


```
. corr week*  
(obs=20)
```

	week	week2	week3
week	1.0000		
week2	0.9713	1.0000	
week3	0.9221	0.9865	1.0000

*4.6 Correlation between week and week2 is 0.97
end of do-file*