

# Practical for Session 4

## Hypothesis Testing

18/10/2011



## 1 Inference about a proportion

Out of 80 women in a random sample of women in Manchester, 13 were asthmatic; this could be used to calculate a 95% confidence interval for the proportion of women in Manchester with asthma. This confidence interval could be compared to the suggested prevalence of 20% in Northern England. An alternative approach would be to test the hypothesis that the true proportion,  $\pi$ , is 0.20.

1.1 What is the expected proportion of women with asthma under the null hypothesis ?  
*0.2*

1.2 What is the observed proportion of women with asthma ? *13/80 = 0.1625*

1.3 What is the standard error of the expected proportion (remember from last week that the standard error of a proportion  $p$  is given by

$$\sqrt{\frac{p(1-p)}{n}}$$

$$\sqrt{\frac{0.2 \times 0.8}{80}} = 0.0447$$

1.4 The appropriate test statistic,  $T$ , is given by the formula:

$$\frac{\text{observed proportion} - \text{expected proportion}}{\text{standard error of proportion}}$$

Calculate  $T$ .

$$T = \frac{0.1625 - 0.2}{0.0447} = -0.839$$

1.5  $T$  should be compared to a t-distribution with how many degrees of freedom ? *79*

1.6 From tables for the appropriate t-distribution, the corresponding  $p$ -value is 0.4. Is it reasonable to suppose that these women are a random sample from a population in which the prevalence of asthma is 20% ? *Yes*

## 2 More inference about a proportion

In the sample heights and weights we have looked at, there were 412 individuals of whom 234 were women. We wish to test that there are equal numbers of men and women in our population.

2.1 What is the null hypothesis proportion of women ? *0.5*

2.2 What is the observed proportion of women ?

$$\frac{234}{412} = 0.568$$

2.3 What is the null hypothesis standard error for the proportion of women ?

$$\sqrt{\frac{0.5 \times 0.5}{412}} = 0.0246$$

2.4 What is an appropriate statistic for testing the null hypothesis ?

$$T = \frac{0.568 - 0.5}{0.0246} = 2.76$$

### 3 Inference about a mean

Load `htwt.dta` into stata with the commands (each command needs to be entered on a separate line).

```
global datadir http://personalpages.manchester.ac.uk/staff/mark.lunt/stats
use $datadir/2_summarizing_data/data/htwt.dta
```

We wish to test whether the mean height is the same in men and women.

3.1 What is the null hypothesis difference in height between men and women ?

*0*

3.2 Use the command `ttest nurseht, by(sex)` to test whether the mean height differs between men and women.

3.3 What is the mean height in men ?

*173.0cm*

3.4 What is the mean height in women ?

*159.8cm*

3.5 What is the mean difference in height between men and women, with its 95% confidence interval ?

*-13.2cm, 95z% CI -14.5cm, -11.9cm,*

3.6 Which of the three hypothesis tests is the appropriate one in this instance ?

*Ha: diff != 0: two sided test that there is a difference*

3.7 What is the p-value from the t-test ?

*less than 0.0001*

- 3.8 What would you conclude ?  
*Men are very significantly taller than women*

## 4 Two-sample t-test

Compare BMI (based on the measured values, i.e. `bmi`) between men and women in `htwt.dta`, using the command `ttest bmi, by(sex)`.

- 4.1 Is there a difference in BMI between men and women ? *Yes, but it is small and not statistically significant*
- 4.2 What is the mean difference in BMI between men and women and its 95% confidence interval.  
*-0.5kg/m<sup>2</sup>, 95%CI -1.4kg/m<sup>2</sup>, 0.4kg/m<sup>2</sup>*
- 4.3 Is there a difference in the standard deviation of BMI between men and women ? (This can be tested with the command `sdtest bmi, by(sex)`)  
*Yes: the standard deviation is significantly greater in women than it is in men*
- 4.4 If there is, repeat the t-test you performed above, using the `unequal` option. Are your conclusions any different ?  
*No: the standard error changes only very slightly, the difference remains non-significant*

## 5 One sample t-test

Load the `bpwide` dataset into stata with the command `sysuse bpwide`. This consists of fiction blood pressure data, taken before and after an intervention. We wish to determine whether the intervention had affected the blood pressure.

- 5.1 Use the `summarize` command to calculate the mean blood pressure before and after the intervention. Has the blood pressure increased or decreased ?  
*Decreased: mean is 156 before, 151 after.*
- 5.2 Generate a variable containing the change in blood pressure using the command `gen bp_diff = bp_after - bp_before`
- 5.3 Use the command `ttest bp_diff = 0` to test whether the change in blood pressure is statistically significant. Is it ?  
*Yes: p = 0.0011*
- 5.4 Give a 95% confidence interval for the change in blood pressure.  
*-8.1, -2.1*

## 6 Power Calculations

The following questions can all be answered using the `sampsi` command.

- 6.1 How many subjects would need to be recruited to have 90% power to detect a difference between unexposed and exposed subjects if the prevalence of the condition is 25% in the unexposed and 40% in the exposed, assuming equal numbers of exposed and unexposed subjects ?  
*432: 216 in each group*
- 6.2 If the exposure was rare, so it was decided to recruit twice as many unexposed subjects as exposed subjects, how many subjects would need to be recruited ?  
*482: 161 exposed and 321 unexposed*
- 6.3 Suppose it were only possible to recruit 100 subjects in each group. What power would the study then have ? *56%*
- 6.4 Suppose that we expect a variable to have a mean of 15 and an SD of 5 in group 1, and a mean of 17 and an SD of 6 in group 2. How large would two equal sized groups need to be to have 90% power to detect a difference between the groups ?  
*161 subjects in each group*
- 6.5 If we wanted 95% power, how large would the groups have to be ?  
*199 in each group*
- 6.6 Suppose we could only recruit 100 subjects in group 1. How many subjects would we have to recruit from group 2 to have 90% power ?  
*276*

*Hint:* the last question can only be answered by trying different numbers for the size of group 2 and seeing what power is achieved. Sensible choice of numbers will give a result fairly quickly. The PageUp key is your friend.

## 7 Stata Log File

```
. global datadir http://personalpages.manchester.ac.uk/staff/mark.lunt/stats
. use $datadir/2_summarizing_data/data/htwt.dta
. ttest nurseht, by(sex)
Two-sample t test with equal variances
```

Group	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
female	227	159.774	.4247034	6.398803	158.9371	160.6109
male	175	172.9571	.5224808	6.911771	171.9259	173.9884
combined	402	165.5129	.4642267	9.307717	164.6003	166.4256
diff		-13.18313	.6666327		-14.49368	-11.87259

```

diff = mean(female) - mean(male)          t = -19.7757
Ho: diff = 0                             degrees of freedom = 400
Ha: diff < 0                             Ha: diff != 0          Ha: diff > 0
Pr(T < t) = 0.0000                       Pr(|T| > |t|) = 0.0000   Pr(T > t) = 1.0000
```

```

. ttest bmi, by(sex)
Two-sample t test with equal variances

```

Group	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
female	225	25.85984	.3268714	4.903072	25.21571	26.50398
male	175	26.35534	.3152409	4.170245	25.73315	26.97753
combined	400	26.07662	.2298956	4.597912	25.62467	26.52858
diff		-.4954959	.4633426		-1.406401	.4154089

```

      diff = mean(female) - mean(male)                t = -1.0694
Ho: diff = 0                                         degrees of freedom = 398
      Ha: diff < 0                Ha: diff != 0                Ha: diff > 0
Pr(T < t) = 0.1428                Pr(|T| > |t|) = 0.2855                Pr(T > t) = 0.8572

. sdtest bmi, by(sex)
Variance ratio test

```

Group	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
female	225	25.85984	.3268714	4.903072	25.21571	26.50398
male	175	26.35534	.3152409	4.170245	25.73315	26.97753
combined	400	26.07662	.2298956	4.597912	25.62467	26.52858

```

      ratio = sd(female) / sd(male)                f = 1.3823
Ho: ratio = 1                                       degrees of freedom = 224, 174
      Ha: ratio < 1                Ha: ratio != 1                Ha: ratio > 1
Pr(F < f) = 0.9874                2*Pr(F > f) = 0.0253                Pr(F > f) = 0.0126

. ttest bmi, by(sex) unequal
Two-sample t test with unequal variances

```

Group	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
female	225	25.85984	.3268714	4.903072	25.21571	26.50398
male	175	26.35534	.3152409	4.170245	25.73315	26.97753
combined	400	26.07662	.2298956	4.597912	25.62467	26.52858
diff		-.4954959	.4541164		-1.388285	.397293

```

      diff = mean(female) - mean(male)                t = -1.0911
Ho: diff = 0                                         Satterthwaite's degrees of freedom = 394.793
      Ha: diff < 0                Ha: diff != 0                Ha: diff > 0
Pr(T < t) = 0.1379                Pr(|T| > |t|) = 0.2759                Pr(T > t) = 0.8621

. sysuse bpwide
(fictional blood-pressure data)

. summarize bp*

```

Variable	Obs	Mean	Std. Dev.	Min	Max
bp_before	120	156.45	11.38985	138	185
bp_after	120	151.3583	14.17762	125	185

```

. gen bp_diff = bp_after- bp_before

```

```

. ttest bp_diff == 0
One-sample t test

```

Variable	Obs	Mean	Std. Err.	Std. Dev.	[95% Conf. Interval]	
bp_diff	120	-5.091667	1.525736	16.7136	-8.112776	-2.070557

```

      mean = mean(bp_diff)
Ho: mean = 0
      t = -3.3372
      degrees of freedom = 119
      Ha: mean < 0
      Ha: mean != 0
      Ha: mean > 0
Pr(T < t) = 0.0006
Pr(|T| > |t|) = 0.0011
Pr(T > t) = 0.9994

. sampsi 0.25 0.4, power(0.9)
Estimated sample size for two-sample comparison of proportions
Test Ho: p1 = p2, where p1 is the proportion in population 1
      and p2 is the proportion in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      power = 0.9000
      p1 = 0.2500
      p2 = 0.4000
      n2/n1 = 1.00
Estimated required sample sizes:
      n1 = 216
      n2 = 216

. sampsi 0.25 0.4, power(0.9) r(0.5)
Estimated sample size for two-sample comparison of proportions
Test Ho: p1 = p2, where p1 is the proportion in population 1
      and p2 is the proportion in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      power = 0.9000
      p1 = 0.2500
      p2 = 0.4000
      n2/n1 = 0.50
Estimated required sample sizes:
      n1 = 321
      n2 = 161

. sampsi 0.25 0.4, n(100)
Estimated power for two-sample comparison of proportions
Test Ho: p1 = p2, where p1 is the proportion in population 1
      and p2 is the proportion in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      p1 = 0.2500
      p2 = 0.4000
sample size n1 = 100
      n2 = 100
      n2/n1 = 1.00
Estimated power:
      power = 0.5618

```

```
. sampsi 15 17, sd1(5) sd2(6) power(.90)
Estimated sample size for two-sample comparison of means
Test Ho: m1 = m2, where m1 is the mean in population 1
           and m2 is the mean in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      power = 0.9000
      m1 = 15
      m2 = 17
      sd1 = 5
      sd2 = 6
      n2/n1 = 1.00
Estimated required sample sizes:
      n1 = 161
      n2 = 161
```

```
. sampsi 15 17, sd1(5) sd2(6) power(.95)
Estimated sample size for two-sample comparison of means
Test Ho: m1 = m2, where m1 is the mean in population 1
           and m2 is the mean in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      power = 0.9500
      m1 = 15
      m2 = 17
      sd1 = 5
      sd2 = 6
      n2/n1 = 1.00
Estimated required sample sizes:
      n1 = 199
      n2 = 199
```

```
. sampsi 15 17, sd1(5) sd2(6) n1(100) n2(200)
Estimated power for two-sample comparison of means
Test Ho: m1 = m2, where m1 is the mean in population 1
           and m2 is the mean in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      m1 = 15
      m2 = 17
      sd1 = 5
      sd2 = 6
sample size n1 = 100
              n2 = 200
              n2/n1 = 2.00
Estimated power:
      power = 0.8621
```

```
. sampsi 15 17, sd1(5) sd2(6) n1(100) n2(280)
Estimated power for two-sample comparison of means
Test Ho: m1 = m2, where m1 is the mean in population 1
           and m2 is the mean in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      m1 = 15
      m2 = 17
      sd1 = 5
      sd2 = 6
sample size n1 = 100
              n2 = 280
              n2/n1 = 2.80
Estimated power:
      power = 0.9016
```

```

. sampsi 15 17, sd1(5) sd2(6) n1(100) n2(275)
Estimated power for two-sample comparison of means
Test Ho: m1 = m2, where m1 is the mean in population 1
           and m2 is the mean in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      m1 = 15
      m2 = 17
      sd1 = 5
      sd2 = 6
sample size n1 = 100
           n2 = 275
           n2/n1 = 2.75
Estimated power:
      power = 0.8998

```

```

. sampsi 15 17, sd1(5) sd2(6) n1(100) n2(277)
Estimated power for two-sample comparison of means
Test Ho: m1 = m2, where m1 is the mean in population 1
           and m2 is the mean in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      m1 = 15
      m2 = 17
      sd1 = 5
      sd2 = 6
sample size n1 = 100
           n2 = 277
           n2/n1 = 2.77
Estimated power:
      power = 0.9005

```

```

. sampsi 15 17, sd1(5) sd2(6) n1(100) n2(276)
Estimated power for two-sample comparison of means
Test Ho: m1 = m2, where m1 is the mean in population 1
           and m2 is the mean in population 2
Assumptions:
      alpha = 0.0500 (two-sided)
      m1 = 15
      m2 = 17
      sd1 = 5
      sd2 = 6
sample size n1 = 100
           n2 = 276
           n2/n1 = 2.76
Estimated power:
      power = 0.9002

```