

Measurement of Cerebral Metabolic Rates of Glucose CMR_{glc} with [^{18}F]FDG PET

A Practical Introduction with References

Rainer Hinz

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Wolfson Molecular Imaging Centre, University of Manchester

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Background: the Irreversible Model for Deoxyglucose

- Sokoloff, L.; Reivich, M.; Kennedy, C.; Des Rosiers, M.H.; Patlak, C.S.; Pettigrew, K.D.; Sakurada, O.; Shinohara, M. The [¹⁴C]deoxyglucose method for the measurement of local cerebral glucose utilization: theory, procedure, and normal values in the conscious and anesthetized albino rat. J. Neurochem. 28 (1977), 897 - 916.
- Reivich, M.; Kuhl, D.; Wolf, A.; Greenberg, J.; Phelps, M.; Ido, T.; Casella, V.; Fowler, J.; Hoffman, E.; Alavi, A.; Som, P.; Sokoloff, L. The [¹⁸F]fluorodeoxyglucose method for the measurement of local cerebral glucose utilization in man. Circ. Res. 44 (1979), 127 - 137.



Combined Forward Rate Constant

$$K_I = \frac{K_1 \cdot k_3}{k_2 + k_3}$$

Cerebral Metabolic Rate of Glucose

$$CMR_{glc} = \frac{C_p}{LC} \cdot K_I$$

Value of the Lumped Constant

$$LC = 0.48$$

'Gold Standard' Measurement of CMR_{glc} for Clinical Research

- Hu, M.T.M.; Taylor-Robinson, S.D.; Ray Chaudhuri, K.; Bell, J.D.; Labbé, C.; Cunningham, V.J.; Koeppe, M.J.; Hammers, A.; Morris, R.G.; Turjanski, N.; Brooks, D.J. [Cortical dysfunction in non-demented Parkinson's disease patients: A combined \$^{31}P\$ -MRS and \$^{18}F\$ FDG-PET study](#). Brain 123 (2000), 340 - 352.
- Edison, P.; Archer, H.A.; Hinz, R.; Hammers, A.; Pavese, N.; Tai, Y.F.; Hotton, G.; Cutler, D.; Fox, N.; Kennedy, A.; Rossor, M.; Brooks, D.J. [Amyloid, hypometabolism, and cognition in Alzheimer disease. An \$^{11}C\$ PIB and \$^{18}F\$ FDG PET study](#). Neurology 68 (2007), 501 - 508.

Protocol used

1. 60 min dynamic acquisition following intravenous bolus administration of $[^{18}F]FDG$.
2. Continuous monitoring of the arterial whole blood activity concentration with high temporal resolution.
3. On a set of discrete blood samples: measurement of the blood and plasma activity concentration and assay of the plasma glucose concentration.

Analysis performed

1. Generation of the $[^{18}F]FDG$ arterial plasma input function.
2. Calculation of parametric maps of K_t using Spectral Analysis.
3. Conversion of the K_t images into CMR_{glc} images.

The Use of a Standard Input Function

- Takikawa, S.; Dhawan, V.; Spetsieris, P.; Robeson, W.; Chaly, T.; Dahl, R.; Margouleff, D.; Eidelberg, D. [Noninvasive quantitative fluorodeoxyglucose PET studies with an estimated input function derived from a population-based arterial blood curve](#). Radiology 188 (1993), 131 - 136.
- Shiozaki, T.; Sadato, N.; Senda, M.; Ishii, K.; Tsuchida, T.; Yonekura, Y.; Fukuda, H.; Konishi, J. [Noninvasive estimation of FDG input function for quantification of cerebral metabolic rate of glucose: optimization and multicenter evaluation](#). J. Nucl. Med. 41 (2000), 1612 - 1618.
- Lewis, J.; Asselin, M.-C.; Herholz, K.; Hinz, R. [Assessment of standard input functions for dynamic FDG brain PET](#). University of Manchester Biomedical Imaging Institute 3rd Annual Showcase, 8th Nov 2011, Poster 13.

See previous presentation *Input functions in PET* at

<http://personalpages.manchester.ac.uk/staff/Rainer.Hinz/material/petif06.html>

Step 1: Invoke MICKI and Load Data

For Solaris/Linux:
`mmic-sun2:~/data`

For Windows:
`S:\rhinz\data`

`/micki &`

`exe`

1a. Load CoNTinuous Blood File

1b. Load DiSCrete Blood File

1c. Select $[^{18}\text{F}]\text{FDG}$

2. Plot CoNTinuous Blood Curve

3. Plot DiSCrete Blood Samples

4. Create Whole Blood Input Function

5. Plasma-Over-Blood Ratio
 6. Create Total Plasma Input Function

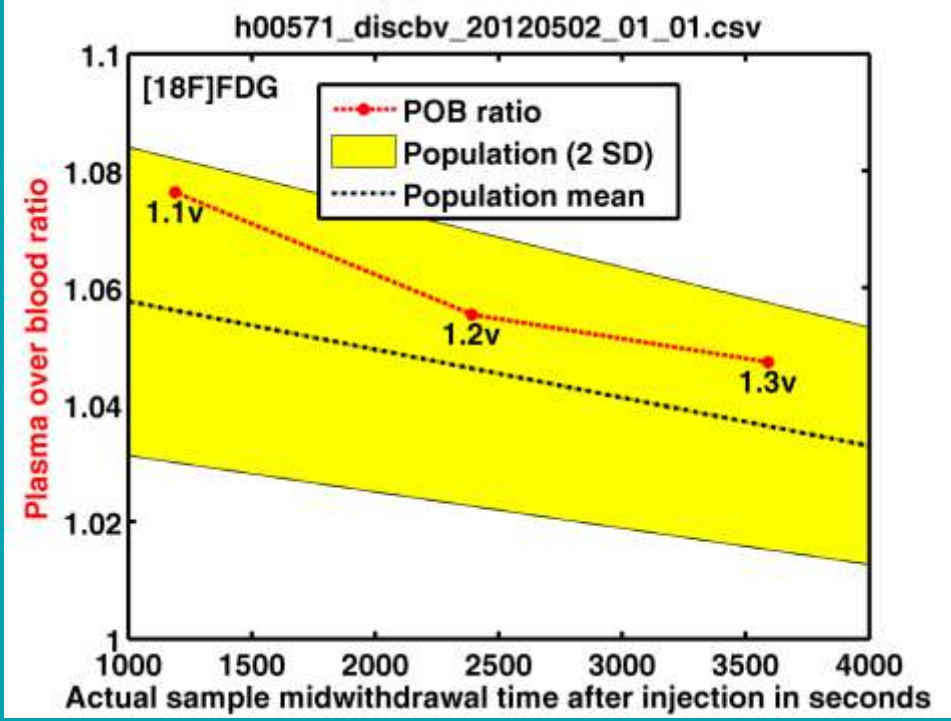
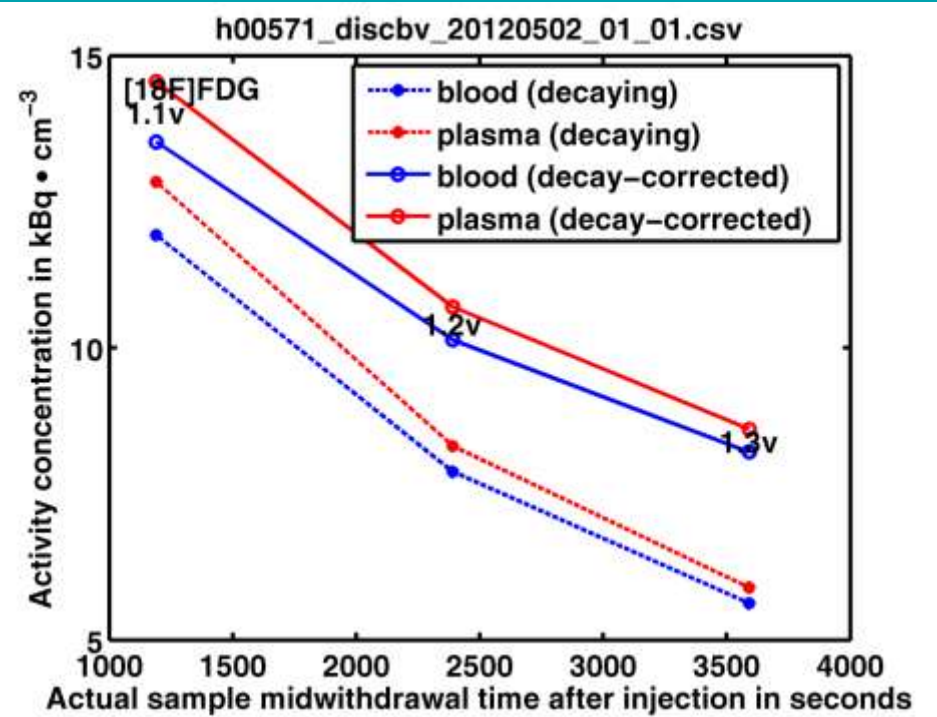
The screenshot shows the MICKI software interface with the following sections and elements:

- Load Data Section:** Contains three buttons: "Load CNT" (with file "fdg_sdf_1.1.csv"), "Load DSC" (with file "h00571_discbv_20120502_01_01_1.csv"), and "Load MET".
- Scan Information Table:**

Subject ID	h00571	
Session ID	01	
Scan ID	01	
Scanner ID	hrrt1	
Scan Start Date	2012-05-02	
Session Protocol ID	58.1	
Scan Start Time	10:11:53	
Administration Time	10:18:53	
Reference Time	injection	injection
Blood Source	arterial	venous
Decay Correction	sampling	sampling
Decay Constant	0.0001053	0.0001053
Last Calibration Sample		
- Validate Data Section:** Contains a radio button for "[^{18}F]FDG" (selected), and two buttons: "Plot CNT" and "Plot DSC".
- Process Data Section:** Contains two buttons: "Totalblood IF" (with file "h00571_tbl_20120502_01_01.csv") and "Totalplasma IF" (with file "h00571_tpl_20120502_01_01.csv").

Step 3: Plot Discrete Blood Samples

1. Measured Activity Concentrations



2. Plasma-Over-Blood Ratios on top of a historic data base from 69 scans (mostly arterial samples)

Step 4: Create Whole Blood Input Function

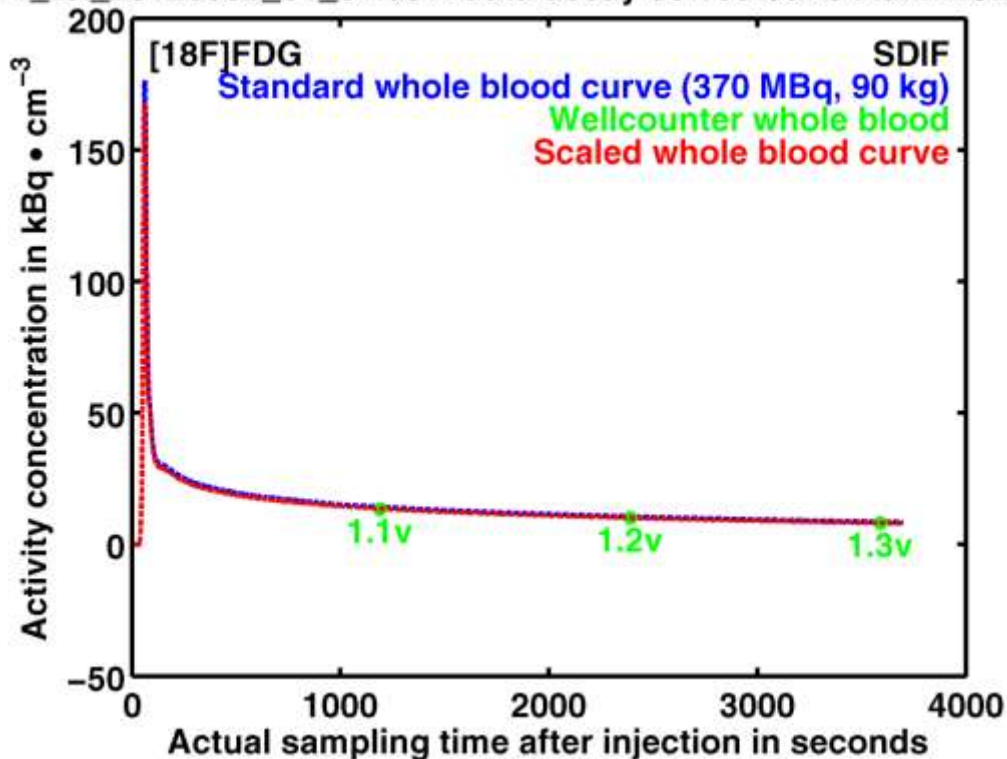
***** STANDARD INPUT FUNCTION SCALE FACTORS *****

wc.time	wc.blood	time	blood	sf_wb	c
1189.5	13.5235	1189	14.3317	0.943607	0
2390.5	10.1368	2390	10.6707	0.949965	1
3590.5	8.21679	3590	8.63504	0.951564	1

NOTE: code= 1 stands for data points selected for fitting

=====
 Scale factor whole bl.: 0.950765
 =====

71_tbl_20120502_01_01.csv: data decay corrected to Administratic



1. Blue curve: scaled using injected dose and body weight only (Shiozaki et al., 2000)
2. Red curve: scaled using the discrete whole blood activity measurements from 37.5 min p.i. onwards (Takikawa et al., 1993)

Step 5: Plasma-Over-Blood Ratio

***** PLASMA-OVER-BLOOD MODEL *****

i	d	w	c
1189.5	1.07631	6.05143	2
2390.5	1.05543	4.67271	2
3590.5	1.04731	3.83214	2

NOTE: code= 2 stands for data points selected for fitting

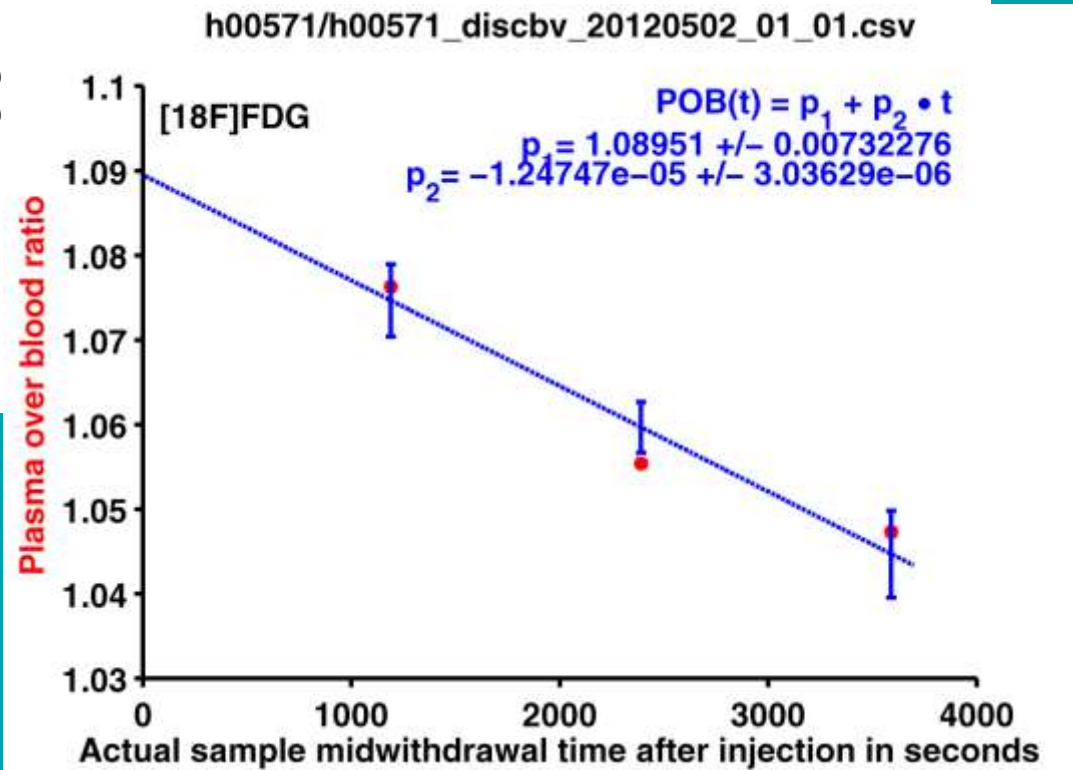
=====

```
res sum squares..... 1.2683016599
res mean square..... 1.2683016599
degrees freedom..... 1
```

=====

```
0 --- 1.0895071332210E+00 +/-
1 --- -1.2474694722886E-05 +/-
```

Straight line fit of all measured samples: slope $\approx -1 \cdot 10^{-5} \text{ s}^{-1}$



Step 6: Create Total Plasma Input Function

Agreement between the discrete plasma samples and the plasma input function

wc.time	wc.plasma	inpfm.time	inpfm.plasma	wc.plasma/inpfm.plasma
1189.5	14.5555	1189	14.6436	0.993984
2390.5	10.6987	2390	10.7509	0.99514
3590.5	8.60556	3590	8.57706	1.00332

Administration Time (DSC) - Scan Start Time (DSC) = 420.000 s

"h00571_tpl_20120502_01_01.csv" written.

"h00571_01_01_cnt.fig" saved.

"h00571_01_01_dsc.fig" saved.

"h00571_01_01_pob.fig" saved.

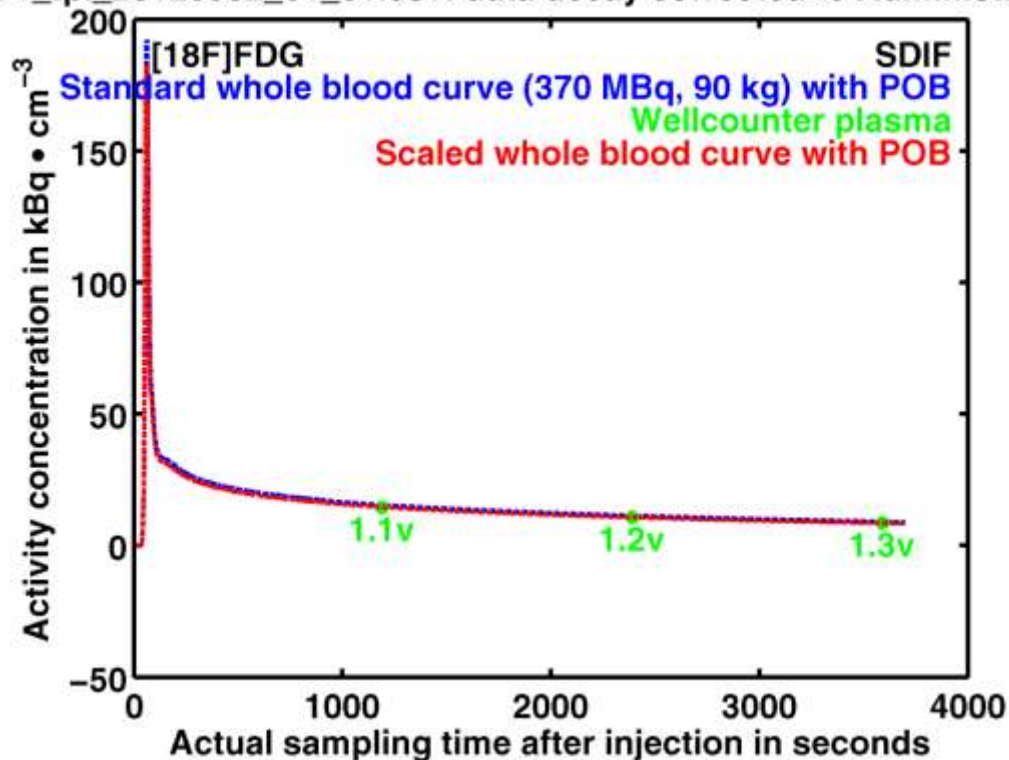
"h00571_01_01_tbl.fig" saved.

"h00571_01_01_pobfit.fig" saved.

"h00571_01_01_tpl.fig" saved.

Plain text file "micki_6.7.log" sav

71_tpl_20120502_01_01.csv: data decay corrected to Administratic



1. Blue curve: scaled using injected dose and body weight only (Shiozaki et al., 2000)
2. Red curve: scaled using the discrete samples (Takikawa et al., 1993) – double that check plasma scale factors are 0.99 ... 1.01

The Estimation of the Combined Forward Rate Constant

In the first instance, developed for region of interest (ROI) analysis

- Gjedde, A. High- and low-affinity transport of D-glucose from blood to brain. *J. Neurochem.* 36 (1981), 1463 - 1471.
- Patlak, C.S.; Blasberg, R.G.; Fenstermacher, J.D. Graphical evaluation of blood-to-brain transfer constants from multiple-time uptake data. *J. Cereb. Blood Flow Metab.* 3 (1983), 1 - 7.
- Patlak, C.S.; Blasberg, R.G. Graphical evaluation of blood-to-brain transfer constants from multiple-time uptake data. Generalizations. *J. Cereb. Blood Flow Metab* 5 (1985), 584 - 590.
- Wong, D.F.; Gjedde, A.; Wagner, H.N. Jr. Quantification of neuroreceptors in the living human brain. I. Irreversible binding of ligands. *J. Cereb. Blood Flow Metab.* 6 (1986), 137 - 146.
- Cunningham, V.J.; Jones, T. Spectral analysis of dynamic PET Studies. *J. Cereb. Blood Flow Metabol.* 13 (1993), 15 - 23.
- Turkheimer, F.; Moresco, R.M.; Lucignani, G.; Sokoloff, L.; Fazio, F.; Schmidt, K. The use of spectral analysis to determine regional cerebral glucose utilization with positron emission tomography and [^{18}F]fluorodeoxyglucose: theory, implementation, and optimization procedures *J. Cereb. Blood Flow Metab.* 14 (1994), 406 - 422.

The Estimation of the Combined Forward Rate Constant

Modifications and extensions for the generation of parametric images of K_1

- Blomqvist, G. [On the construction of functional maps in positron emission tomography](#). J. Cereb. Blood Flow Metab. 4 (1984), 629 - 632.
- Tadokoro, M.; Jones, A.K.P.; Cunningham, V.J.; Sashin, D.; Grootoink, S.; Ashburner, J.; Jones, T. Parametric images of ^{11}C -diprenorphine binding using spectral analysis of dynamic PET images acquired in 3D. *In: Quantification of Brain Function: Tracer Kinetics and Image Analysis in Brain PET* (Uemura K, Jones T, Lassen NA, Kanno I, eds), New York: Excerpta Medica, 289 - 294.
- Turkheimer, F.E.; Aston, J.A.D.; Asselin, M.-C., Hinz, R. [Multi-resolution Bayesian regression in PET dynamic studies using wavelets](#). Neuroimage 32 (2006), 111 - 121.
- Hinz, R.; Edison, P.; Brooks, D.J.; Turkheimer, F.E. [Multi-resolution Bayesian regression for parametric imaging of \[\$^{18}\text{F}\$ \]FDG brain studies](#). J. Cereb. Blood Flow Metab. 27 (2007), Supplement 1, PO04-04U.

See full presentation *Multi-resolution Bayesian regression for parametric imaging of [^{18}F]FDG brain studies* at

<http://personalpages.manchester.ac.uk/staff/Rainer.Hinz/material/osaka07.html>

Conversion of K_f images into CMRglc images

```
For Solaris/Linux:
mmic-sun2:~/data/fdg/t00321> cmrgima t00321_45min.hdr

Input file      : "t00321_45min.hdr" (type 0)
  ROIScale     = 3.0592648e-08 = 0x330364f9 (single precision)
  cal_max      = 1.0024293e-03 = 0x3a8363f2 (single precision)
```

Enter Plasma Glucose Samples in Millimolar Units (concentration in mmol/l):

```
*** press Ctrl-D (^D) to finish input ***
  Sample 0     = 5.70
  Sample 1     = 5.54
  Sample 2     = 5.50
  Sample 3     = 5.36
  Sample 4     = 5.50
  Sample 5     = done.
  Mean         = 5.520000000000000e+00 mmol/l
  Lumped Con= 0.48
Output Image= Input Image * 1.150000000000000e+01 * 60
ROIScale     = 2.110892712000000e-05 (double precision)
cal_max      = 6.916762170000000e-01 (double precision)

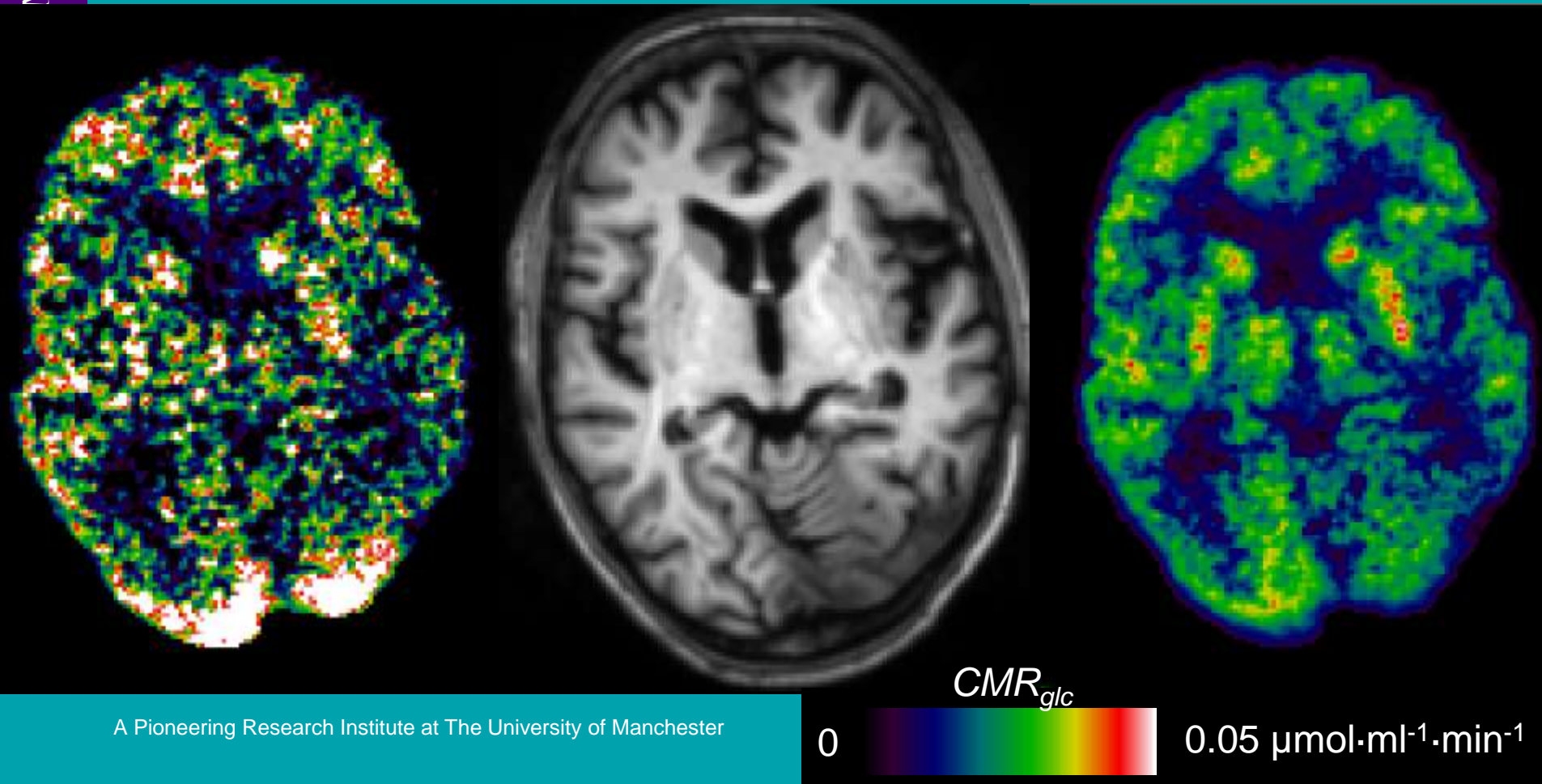
Output files  : "./t00321_45min_cmrg.img" -> written.
               "./t00321_45min_cmrg.hdr" -> written.
  ROIScale     = 2.1108926e-05 = 0x37b11313 (single precision)
  cal_max      = 6.9167620e-01 = 0x3f3111b1 (single precision)
```

<http://personalpages.manchester.ac.uk/staff/Rainer.Hinz/material/toolshelp.html#cmrgima>

CMR_{glc} measured on the HRRT in Manchester

Graphical Analysis (Gjedde-Patlak Plot),
Slope
(5 frames: 35 min ... 60 min, 5 % blood volume)

Spectral Analysis,
45 min Impulse Response Function (IRF)
(28 frames)



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